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A new stabilization based on the mass matrix for Biot's consolidation model

Álvaro Pé de la Riva¹, Carmen Rodrigo², Francisco J. Gaspar³

SUMMARY

A stabilization is usually required in order to avoid nonphysical oscillations in the numerical solution of the fluid pressure for the quasi-static Biot's model for poroelasticity [1]. For this purpose, we propose to add a mass term as stabilization such that the spurious oscillations are completely eliminated. In addition, this stabilization can be applied in a natural way together with the well-known fixed-stress method [2] for solving the poroelasticy problem. In this work, we will consider pairs of isogeometric elements for discretization. Specifically, we propose the pairs of isogeometric elements Q1 - Q1, Q2 - Q1 and Q3 - Q2 (with global C^1 smoothness). By means of the standard von Neumann analysis, we prove the stability and convergence of these schemes. Finally some numerical results will be shown.

Keywords: Poroelasticity, Biot's model, stabilization, von Neumann analysis, isogeometric analysis

AMS Classification: 65F10, 65L20

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¹IUMA, Department of Applied Mathematics University of Zaragoza email: apedelariva@unizar.es

²IUMA, Department of Applied Mathematics University of Zaragoza email: carmenr@unizar.es

³IUMA, Department of Applied Mathematics University of Zaragoza email: fjgaspar@unizar.es