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CoPO, the Corrector of Periodic Orbits algorithm with high precision.

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SUMMARY

In this talk the CoPO (cf. [1]) algorithm is presented. This corrector algorithm computes up to any arbitrary precision periodic orbits of dynamical systems. It is based on an optimized shooting method combined with a numerical ODE solver, TIDES (cf. [2]), that uses a Taylor series method. This methodology is nowadays the only one capable to reach precisions up to 1000 digits or more. Moreover, some numerical tests for the Henon-Heiles' Hamiltonian and the Lorenz's model which show the good behavior of the proposed method are presented. Finally, a data base (cf. [3]) of rigorous and high precision periodic orbits of the Lorenz model is exposed.

Keywords: Periodic Orbits, shooting method, Taylor series method, Lorenz model.

AMS Classification: 37M20, 65P20

References

- ABAD, ALBERTO AND BARRIO, ROBERTO AND DENA, ANGELES. Computing periodic orbits with arbitrary precision. *Physical review. E* 84(016701), 1–6, 2011.
- [2] A. ABAD, R. BARRIO, F. BLESA Y M. RODRGUEZ. Algoritmo 924: TIDES, un integrador de la serie Taylor para ecuaciones diferenciales. ACM Transactions on Mathematical Software (TOMS) 39(1), 5:1–5:28, 2012.
- [3] R. BARRIO, A. DENA Y W. TUCKER. A database of rigorous and high-precision periodic orbits of the Lorenz model. *Computer Physics Communications* 194, 76–83, 2015.

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