

Stabilized virtual element method for the incompressible Navier-Stokes equations

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SUMMARY

In this work, we present a stabilized virtual element method (VEM) discretization for the incompressible Navier-Stokes equations. Basically, VEM can be considered a generalization of FEM that enables a polynomial decomposition of the domain. VEM has been applied to elasticity and fluidmechanics differential equations [1, 2, 3]. In this work, the concepts of stabilized methods [4] are introduced in the VEM formulation. Thus, stabilization terms are included in the variational form to circumvent the Babuška-Brezzi condition and to stabilize the solution for convection dominated flows. Numerical examples are presented to show the behavior of the method.

Keywords: VEM, Navier-Stokes equations, Stabilized methods

AMS Classification: 76D05, 65M60

References

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