

# Analyticity of the semi-group generated by the Stokes operator with Navier-type boundary conditions on $L^p$ -spaces

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## SUMMARY

We prove here the analyticity of the Semi-group generated by the Stokes operator with Navier-type boundary conditions on  $L^p$ -spaces. This analyticity allows us to solve the linearised evolution Navier-Stokes problem with Navier-type boundary conditions

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial t} - \Delta \mathbf{u} + \nabla \pi = \mathbf{f}, & \operatorname{div} \mathbf{u} = 0 & \text{in } \Omega \times (0, T), \\ \mathbf{u} \cdot \mathbf{n} = 0, & \operatorname{curl} \mathbf{u} \times \mathbf{n} = \mathbf{0} & \text{on } \Gamma \times (0, T), \\ \mathbf{u}(0) = \mathbf{u}_0 & & \text{in } \Omega. \end{cases}$$

**Keywords:** Analytic semi-group, Stokes operator, Navier-type boundary condition,  $L^p$ -spaces,...

**AMS Classification:** Primary 35Q30, 76D05, 76D07, 35K20, 35K22 ; Secondary 76N10, 35A20, 35Q40

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